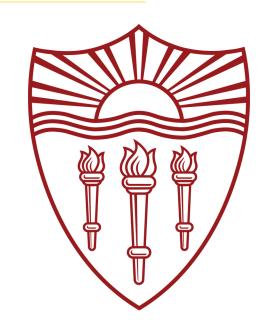
Weakly Deterministic Characterizations of Unbounded Tonal and Featural Spreading

SCAMP April 7, 2018

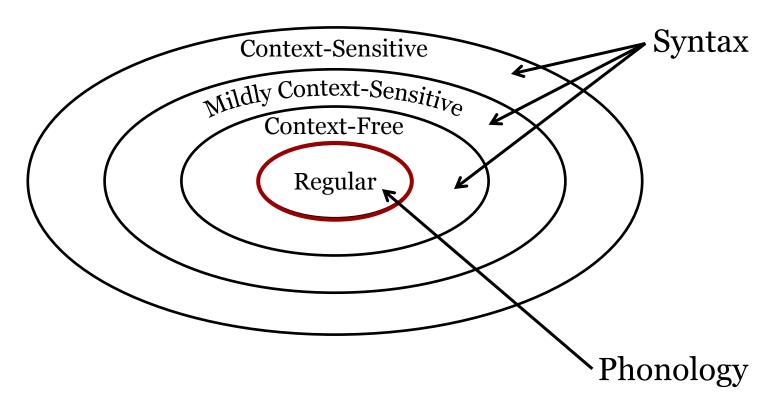
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University of Southern California

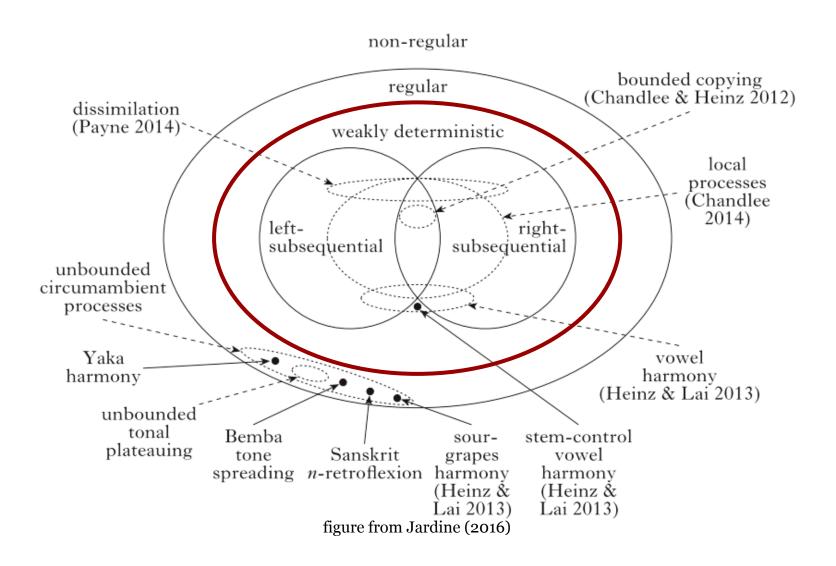


The Chomsky Hierarchy

Languages (sets of strings) can be classified by computational complexity (Chomsky 1956):



The Subregular Hierarchy

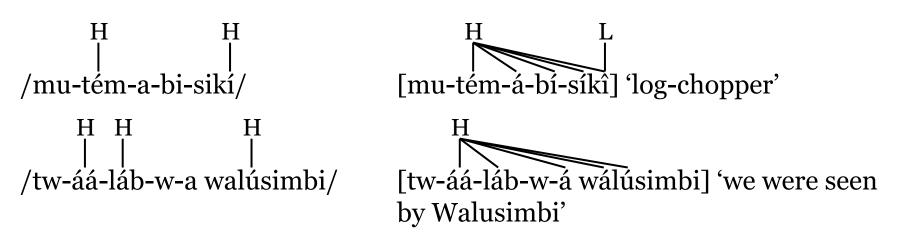


Lango Unbounded Tonal Plateauing

(Hyman & Katamba 2010)

Single high tone does not spread:

 Multiple high tones spread to tone bearing units between them:



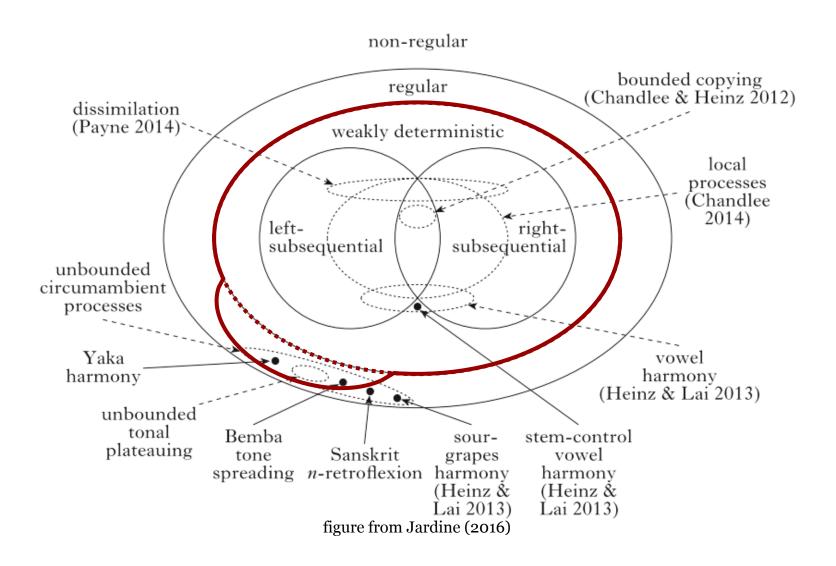
Classifying Featural and Tonal Spreading

- Segmental phenomena are at most weakly deterministic (Heinz & Lai 2013)
- Some tonal phenomena (unbdounded plateauing) are regular, but not weakly deterministic (Jardine 2016)

Proposals:

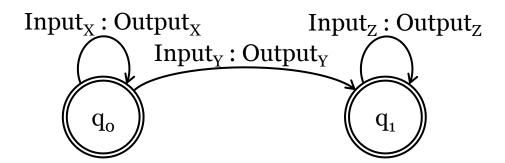
- 1) Attested featural and tonal spreading patterns **are** weakly deterministic
- 2) Unattested patterns (i.e. sour grapes) are **not** weakly deterministic

The Subregular Hierarchy



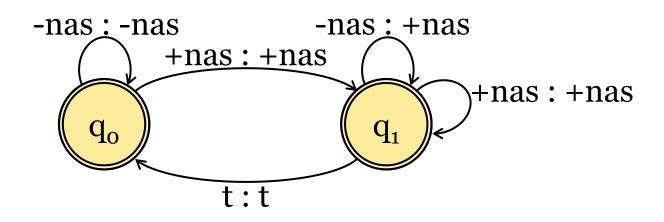
Finite State Transducers

- Input-output mapping of strings can be conceptualized as finite state transducers
- Maps inputs to outputs by following transitions between states



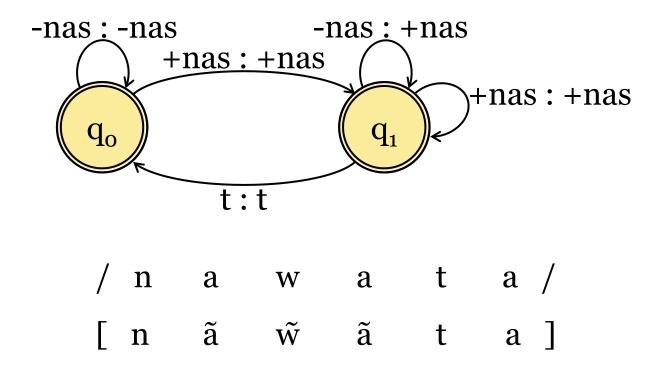
• Finite state transducer indicates which input-output mappings are licit in a language

Progressive Harmony

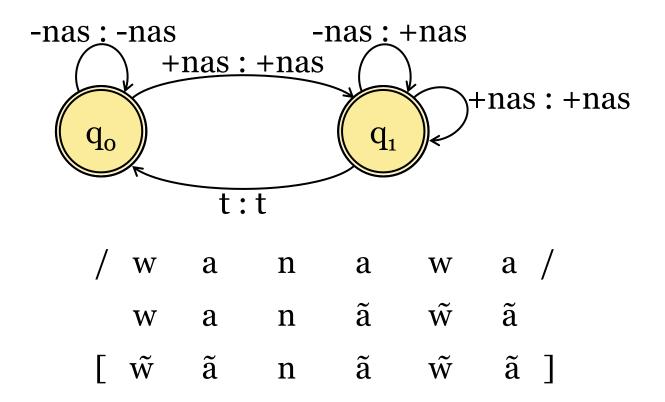


```
/ l a w a / / n a w a / [ l a w a ] [ n ã w̃ ã ]
```

Progressive Harmony

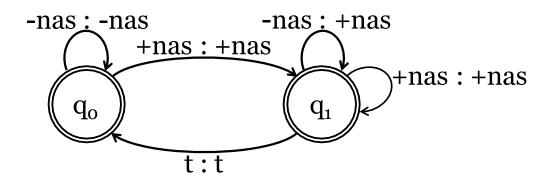


Bidirectional Harmony



Determinism

- Properties of finite state transducers indicate computational complexity of input-output maps
- Deterministic: for a given input symbol, there is only one possible transition



• Non-deterministic: for a given input symbol, there are multiple possible transitions

Weak Determinism

- Unidirectional harmony and bidirectional harmony are weakly deterministic (Heinz & Lai 2013)
- Weakly deterministic maps:
 - Can be decomposed into left- and right-subsequential functions
 - Are alphabet-preserving
 - Are length-preserving

Metaphony (Bounded Harmony)

- Metaphony: post-tonic high vowel targets stressed mid vowel for raising
- Central Veneto (Walker 2005, 2010, 2011)

```
[kant-é-se] 'sing (1sg impf subj)' kant-í-si-mo] 'sing (1pl impf subj)' [órden-o] 'order (1sg)' [úrdin-i] 'order (2sg)'
```

[ángol-o] 'angle (sg)' [ángol-i] 'angle (pl)'

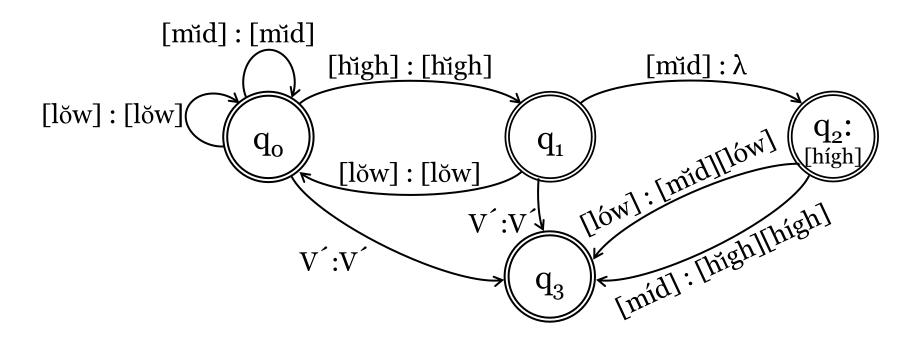
Metaphony (Bounded Harmony)

Metaphony is circumambient:

```
/an . go . l-i/ /or . de . n-o/ /or . de . n-i/ [an . go . l-i] [or . <u>de</u> . n-o] [ur . <u>di</u> . n-i]
```

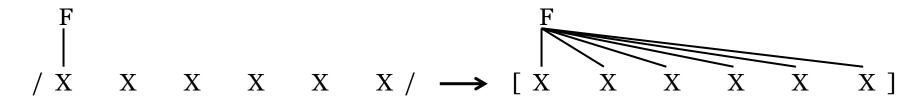
- Vowel's status as undergoer of metaphony determined by material on both sides
- BUT that material is not unboundedly far away

Metaphony (Bounded Harmony)

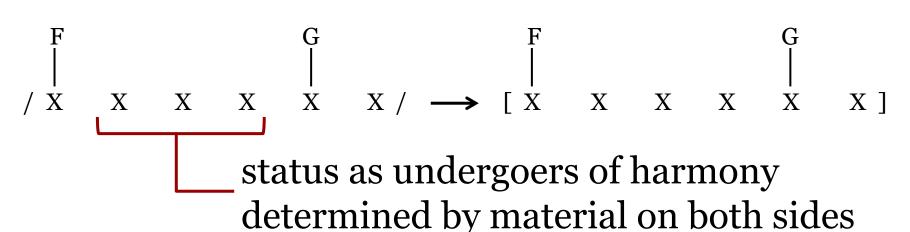


Sour Grapes in Unbounded Feature Spreading

• Full spreading with no blocker present:

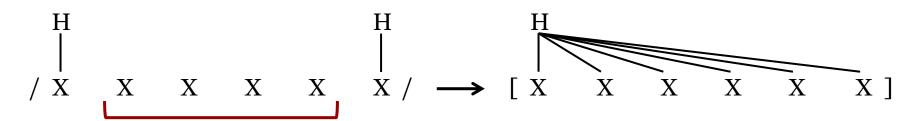


No spreading with blocker present:

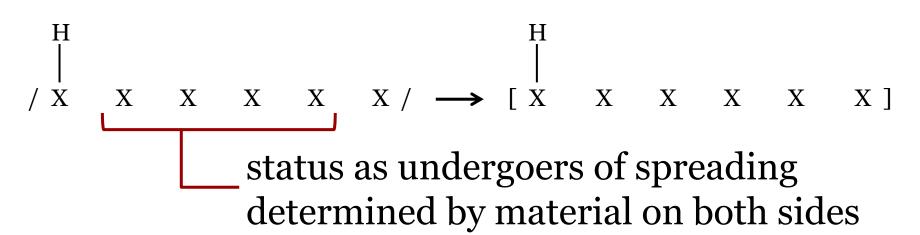


Unbounded Tonal Plateauing

Tonal plateauing between high tones:

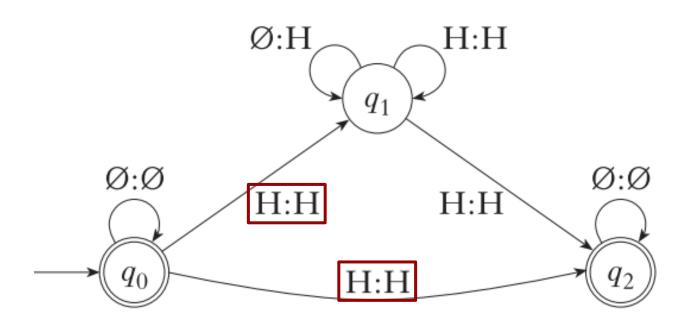


No spreading with single high tone:



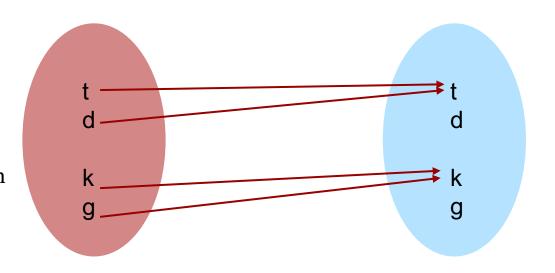
Unbounded Tonal Plateauing & Non-Determinism

Finite state transducer necessary for unbounded tonal plateauing is non-deterministic (Jardine 2016)



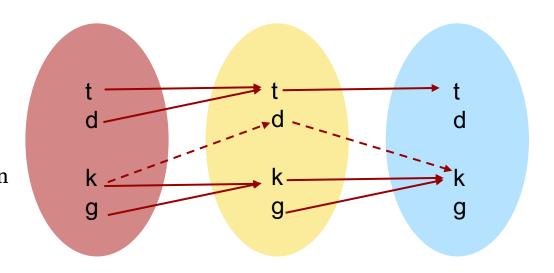
Weak Determinism Allows for Some Markup

- To be weakly deterministic, the first FST cannot add new characters to the alphabet, or increase the length of the word
- But there is still a lot of unused information!
 - Very few phonological patterns are one-to-one (injective)
 - We can mark up positional information on the intermediate representation
- For markup to work, there must be fewer possible surface representations than intermediate representations



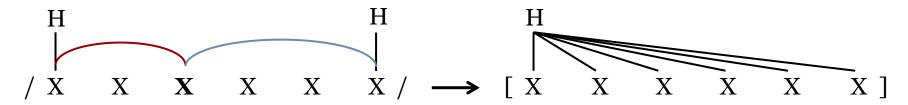
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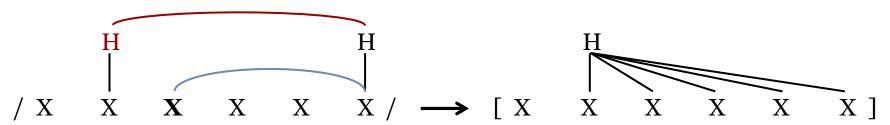


Two Understandings of Unbounded Tonal Plateauing

• Undergoers must precede and follow triggers (from any distance)

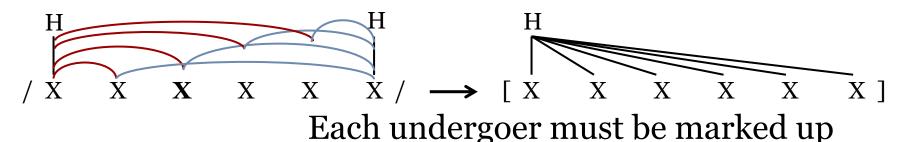


• Undergoers precede a trigger, but not the first trigger

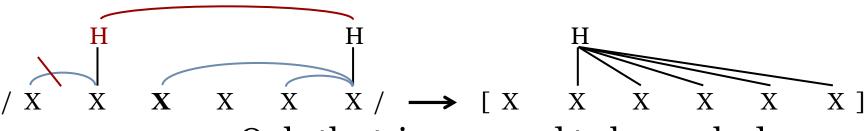


Two Understandings of Unbounded Tonal Plateauing

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• Undergoers precede a trigger, but not the first trigger



Only the triggers need to be marked up

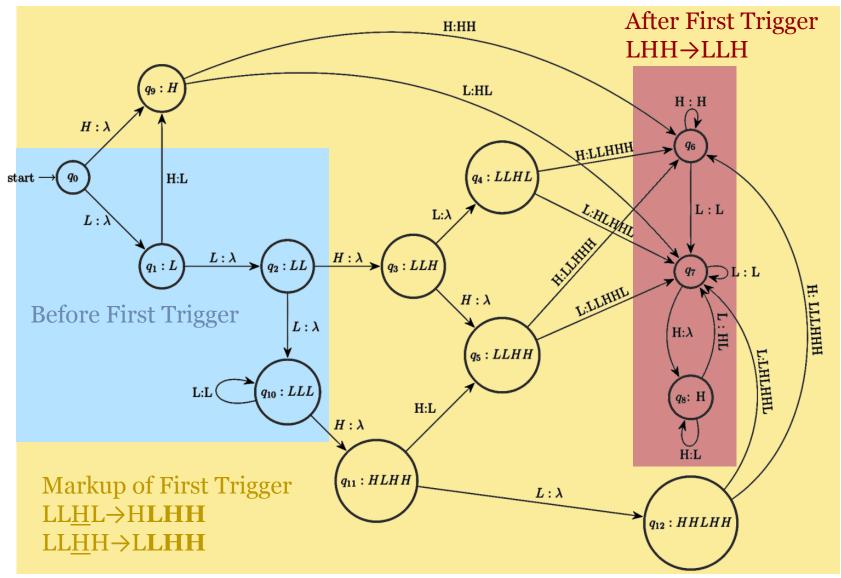
Local Markup Strategy

- All *x* in the alphabet are available on the surface
 - Markup cannot be segmental
- Not all substrings xy are available on the surface
- UTP is attempted with a LFST then a RFST
- Three properties of UTP:
 - Anything preceding the first H, surfaces as L
 - Anything following the final H surfaces as L
 - Anything between the first H and final H surfaces as H
- LFST can mark first H with adjacent TBUs, since they will surface predictably
 - If markup for H is unique, RFST can spread from last H to the first H, by stopping at the markup

Local Markup-LFST

- Marks up first H with LHH
 - #H→#H
 - #LH→#LH
 - LLHL→HLHH
 - LLHH→LLHH
- Makes sure no other LHH appear
 - H...LHH→H...LLH
- This overwrites underlying tone in three places
 - H...L \underline{X} H→H...L \underline{L} H, but \underline{X} will surface as H regardless.
 - HY→HH, could be a problem, so encoded in \underline{Z}
 - $\underline{Z}LH{H,L}$ → $\{L,H\}LHH$, but \underline{Z} must have been L.

Leftward FST



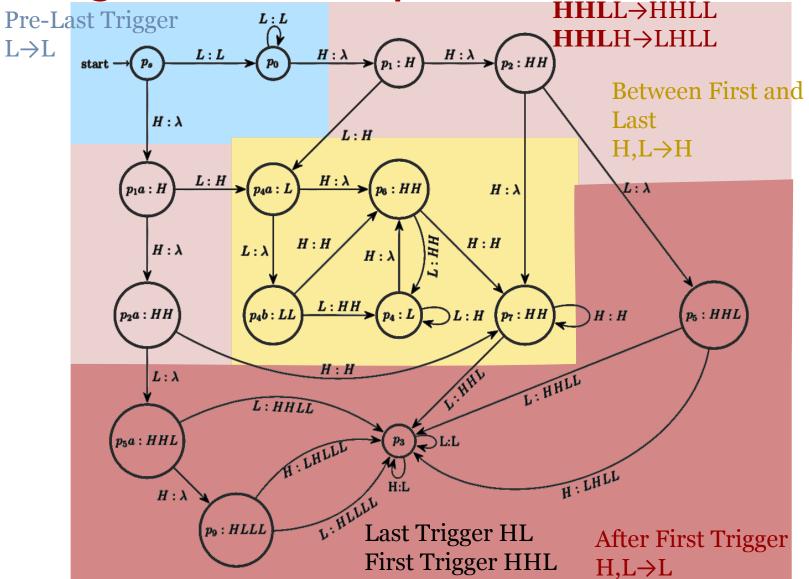
Right FST

- Right FST can identify the last H
- Spreads H from last H until it sees the LHH substring (reversed to HHL).
 - After which, spreads L.
- If the last H is in a LHH substring
 - HLHH→LLHL
 - LLHH→LLHH
- Also, if last H is in #LH, no spreading occurs.

Right-to-Left Spread

 $L \rightarrow L$

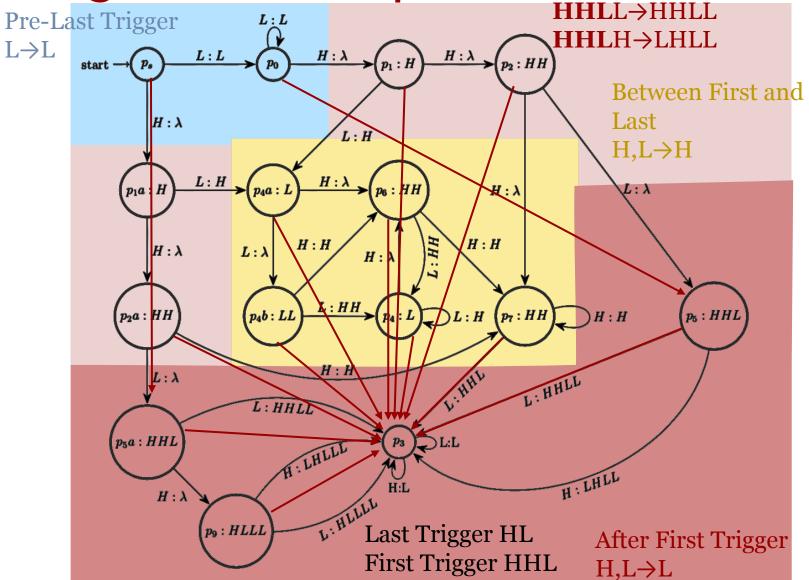
Last Trigger is in First Trigger String



Right-to-Left Spread

 $L \rightarrow L$

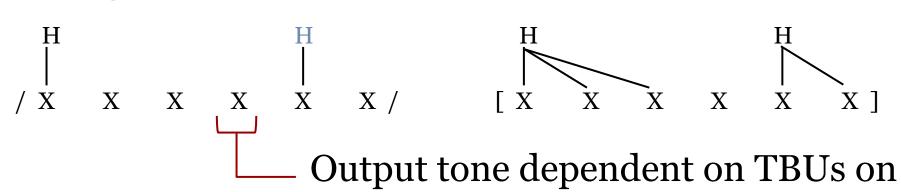
Last Trigger is in First Trigger String



 Full spreading to right edge with no intervening High tone

 Non-iterative spreading with an intervening High tone

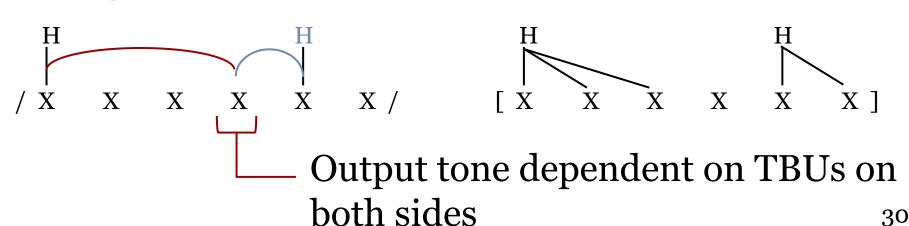
both sides



 Full spreading to right edge with no intervening High tone



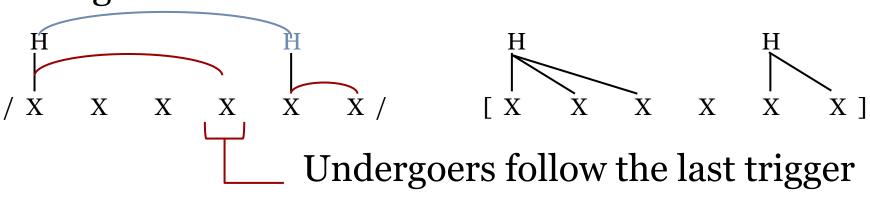
 Non-iterative spreading with an intervening High tone



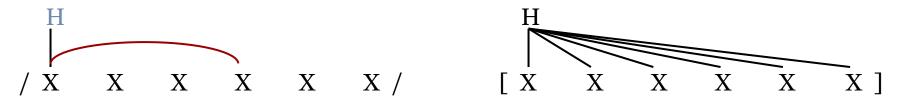
 Full spreading to right edge with no intervening High tone



 Non-iterative spreading with an intervening High tone



 Full spreading to right edge with no intervening High tone



 Non-iterative spreading with an intervening High tone

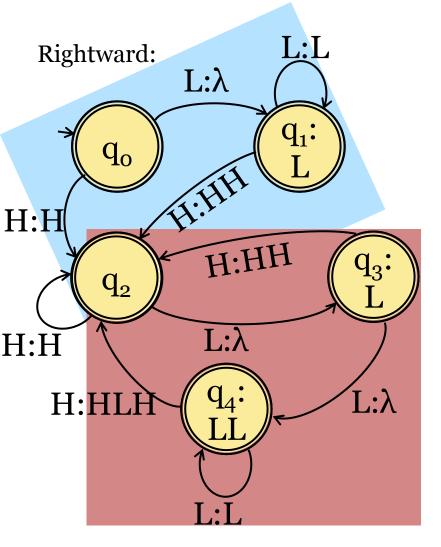


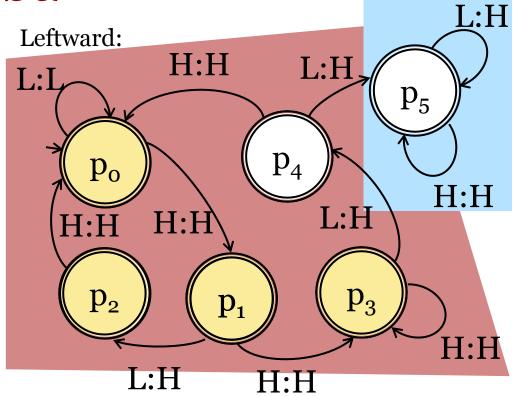
Need to mark up non-last High tones

Copperbelt Bemba Markup

- Non-last H have two predictable TBUs following them
 - -H??... $H \rightarrow HHH...H$ (due to bounded spread)
 - Mark up H??...H as HLH...H
- All TBUs following last H are predictable
 - -H...?→H...H
 - So mark up last H locally HL as HH
- LFST then fills in HLH→HHH, and spreads from HHLL

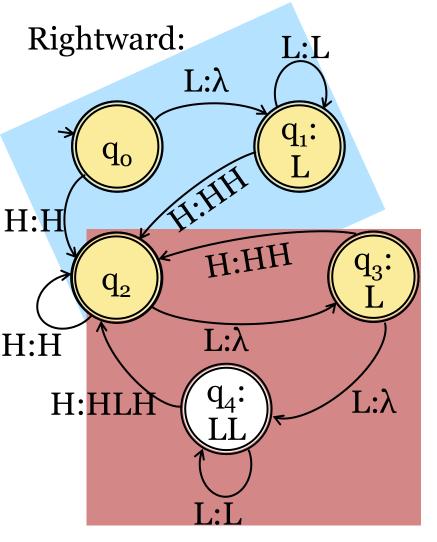
Copperbelt Bemba

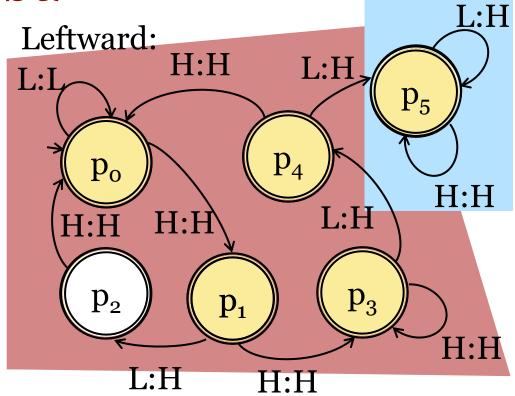




```
/ H L L L H L /
H L H H H
[ H H H L H H ] 3/4
```

Copperbelt Bemba





```
    / H
    L
    H
    L
    L
    L

    H
    H
    H
    H
    L
    L

    [ H
    H
    H
    H
    H
    H
    ]30
```

Results Thus Far

| Tonal Plateauing | First Trigger | Last Trigger |
|-------------------------|------------------------------|--------------------------|
| | XL <u>H</u> H (HL <u>H</u>) | L <u>H</u> (H <u>H</u>) |
| Copperbelt Bemba | Last Triggers | Pre-Blocker Triggers |
| | <u>H</u> HLL | <u>H</u> LH |
| Sour Grapes | Post-Blocker Triggers | Pre-Blocker Triggers |
| | ??? | ??? |

True Sour Grapes Markup

- Before the last H (blocker), there is no spreading
 - Before the blocker, Sour Grapes is one-to-one:
 - H??...H→H??...H

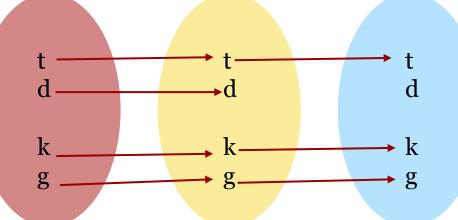
So the markup mapping must be one-to-one before the blocker

True Sour Grapes Markup

- Before the last H (blocker), there is no spreading
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So the markup mapping must be one-to-one before the blocker

Nothing pre-blocker can be marked up



Let's Try: True Sour Grapes Markup

- All TBUs following last H are predictable
 - H...?→H...H
 - Suppose we can mark up H as some string XY
 - If all elements of XY are in the alphabet, XY could appear underlyingly before the last H
 - /XY...HL/→[XY...HH]
 - /XY...HL/ cannot markup to XY...XY, (XY is unique)
 - /XY...HL/ is marked up as $ZW...XY \rightarrow_{LFST} XY...HH$
 - Now ZW...HL cannot markup to ZW...XY
 - Some AB must mark up to XY (markup is injective)
- Contradiction: no such markup exists
- Sour Grapes is not weakly deterministic

Conclusion

• Attested unbounded circumambient processes (tonal and featural) are weakly deterministic

| Tonal Plateauing | First Trigger | Last Trigger |
|------------------|------------------------------|--------------------------|
| | XL <u>H</u> H (HL <u>H</u>) | L <u>H</u> (H <u>H</u>) |
| Copperbelt Bemba | Last Triggers | Pre-Blocker Triggers |
| | <u>H</u> HLL | <u>H</u> LH |
| Sour Grapes | Post-Blocker Triggers | Pre-Blocker Triggers |
| | ??? | ??? |

• Unattested sour grapes patterns are regular, but not weakly deterministic